

Math 1553


Introduction to Linear Algebra

School of Mathematics
Georgia Institute of Technology

Math 1553

Web Sites

Dan Margalit About Team Research Books 1553 Teaching REU




I am a Professor in the School of Mathematics at Georgia Institute of Technology. My research lies in the intersection of low-dimensional topology and geometric group theory. I mainly focus on mapping class groups of surfaces, that is, the symmetries of surfaces. I have published a number of [articles](#) and three [books](#) on these topics.


Some activities I am involved in:

- [Topology Students Workshop](#)
- [Topology Students Resource](#)
- [Algebraic & Geometric Topology](#)
- [Geometry-Topology Seminar \(mailing list\)](#)
- [REU](#)


Conferences and Special Sessions I am currently organizing:

- [Tech Topology Conference](#)
- [Mathematical Congress of the Americas](#)
- [No Boundaries: Groups in Algebra, Geometry, and Topology](#)





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Math 1553
Introduction to Linear Algebra
Fall 2017 — Sections E1 - E5

Georgia Tech

For most course information, see the Math 1553 Master Site:

[Master Course Website](#)

For information specific to Sections E1 - E5, see the syllabus:

[Syllabus](#)

For the Gradebook, Piazza, and WebWork, see T-Square:

[T-Square](#)

For on-line access to the textbook, see MyMathLab (course id: margalit62306):

[MyMathLab](#)

Basic Information

Instructor	Dan Margalit
Lecture time	MW 10:10–11:00am
Lecture location	College of Computing 16
My office	Skiles 234
My email	margalit@math.gatech.edu
Office hours	TBA
Recitation time	F 10:10–11:00am
Recitation location	E1: Skiles 156

Math 1553 E1 - E5 Web Site

people.math.gatech.edu

Course Calendar and Materials

Here is a [reference sheet](#) containing most theorems and definitions that you will learn (and be responsible for knowing) over the course of the semester. It will be tweaked as we cover the material.

Date	Topic	Materials	WeBWorK	Quiz/Exam	Remarks
M Aug 21	Overview	Slides			
W Aug 23	Lines and planes in \mathbb{R}^n and 1.1, Systems of equations				
F Aug 25	Recitation: Lines, planes, 1.1		Warmup		
M Aug 28	1.1 (continued) and 1.2, Row reduction				
W Aug 30	1.2, Row reduction (continued)		1.1		
F Sep 1	Recitation: 1.1, 1.2			Quiz: Lines, planes, 1.1	
M Sep 4	<i>Labor Day</i>				
W Sep 6	1.3, Vectors in \mathbb{R}^n , span		1.2		
F Sep 8	Recitation: 1.3			Quiz: 1.1, 1.2	
M Sep 11	1.4, Matrix equations				
W Sep 13	1.5, Solution sets		1.3		
F Sep 15	Recitation: 1.4, 1.5			Quiz: 1.3	
M Sep 18	1.6, Applications of linear systems				
W Sep 20	Review		1.4, 1.5		

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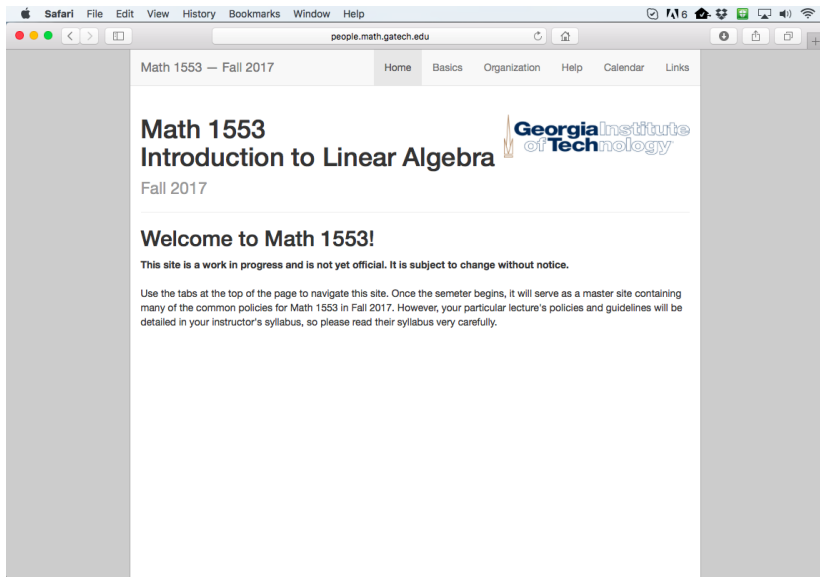
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Math 1553 Master Web Site




The image shows a screenshot of a web browser displaying the Math 1553 Master Web Site. The browser's address bar shows the URL `people.math.gatech.edu`. The page has a navigation menu with links for Home, Basics, Organization, Help, Calendar, and Links. The main content area features the title "Math 1553 Introduction to Linear Algebra" and the Georgia Institute of Technology logo. Below the title, it says "Fall 2017". A prominent heading reads "Welcome to Math 1553!". A notice states: "This site is a work in progress and is not yet official. It is subject to change without notice." A final paragraph explains that the site will serve as a master site for common policies, but individual lecture policies will be detailed in syllabi.

Math 1553 — Fall 2017

Home Basics Organization Help Calendar Links

Math 1553

Introduction to Linear Algebra



Fall 2017

Welcome to Math 1553!

This site is a work in progress and is not yet official. It is subject to change without notice.

Use the tabs at the top of the page to navigate this site. Once the semester begins, it will serve as a master site containing many of the common policies for Math 1553 in Fall 2017. However, your particular lecture's policies and guidelines will be detailed in your instructor's syllabus, so please read their syllabus very carefully.

Plazza Forums for Classrooms

t-square.gatech.edu

My Workspace MATH-1553-E1,E2,E3,E4,E5 MATH-1553-H,J,SPR16 MATH-1553-HP1,HP2_FALL15 My Active Sites View Site As: - Select Role - Logout

COURSE TOOLS

- Home
- Roster
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- Gradebook
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- Piazza
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- Statistics
- Help

SITE INFORMATION DISPLAY

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Safari File Edit View History Bookmarks Window Help

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PIAZZA

1553 Q & A Resources Statistics Manage Class

polls hw1 hw2 hw3 hw4 logistics other

New Post Search or add a post...

PINNED

- Private Search for Teammates! 8/14/17

YESTERDAY

- Instr **Latex Edit** Yesterday 9:21PM
I'd like to point out the Latex equation editor. When you are typing a message, click on the button that says fx.
- Instr **tagging Joe** 9:18PM
Piazza says I can tag instructors. Does this work @Joseph Rabinoff ?
- Private Instr 2:48PM
first try
[o] WS [o] AB

THIS WEEK

- Private Introduce Piazza to your stu... Mon
- Private Get familiar with Piazza Mon
- Private Tips & Tricks for a succesf... Mon
- Welcome to Piazza! Mon
Piazza is a Q&A platform designed to get you great answers from classmates and instructors fast. We've put together thi

note

Latex Editor

I'd like to point out the Latex equation editor. When you are typing a message, click on the button that relatively easy to type math:

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

You just type in regular LaTeX and it shows you a preview on the fly.

logistics other

edit good note 0 Updated

followup discussions for lingering questions and comments

Start a new followup discussion

Compose a new followup discussion

The screenshot shows a web browser window with the URL `t-square.gatech.edu`. The browser's address bar and menu bar are visible. The page header includes navigation tabs for `My Workspace`, `MATH-1553-E1,E2,E3,E4,E5`, `MATH-1553-H,J,SPR16`, `MATH-1553-HP1,HP2_FALL15`, and `My Active Sites`. A `Logout` button is in the top right. A sidebar on the left lists `COURSE TOOLS` including `Home`, `Roster`, `Email`, `Gradebook`, `Webwork`, `Piazza`, `Site Info`, `Statistics`, and `Help`. The main content area is titled `SITE INFORMATION DISPLAY` and features the Georgia Tech logo. The course title is `Math 1553 Introduction to Linear Algebra` for `Fall 2017 — Sections E1 - E5`. The page provides links for `Master Course Website`, `Syllabus`, `T-Square`, and `MyMathLab`. A `Basic Information` section lists the instructor as `Dan Margalit`, the lecture time as `MW 10:10-11:00am`, and the location as `College of Computing 16`.

Plazza Forums for Classrooms

t-square.gatech.edu

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webwork.math.gatech.edu

Joe's Slides TSquare AGT Calendar Toodledo O365 JKG MSN Apple iCloud Yahoo Bing Google Wikipedia Facebook The Weather Channel Yelp TripAdvisor

T-Square : MATH-1553-E1,E2,E3,E4,E5 : Webwork WeBWork : Math-1553_FALL17

  **MAA** MATHEMATICAL ASSOCIATION OF AMERICA

Logged in as
f01272a44a9d65f13cf2e496ab3d8e54.
[Log Out](#)

webwork / Math-1553_FALL17

Math-1553_FALL17

Homework Sets

Name	Status
<input type="checkbox"/> 0.0 Warmup	will open on 08/21/2017 at 12:00am EDT

[Clear](#)

[Download PDF or TeX Hardcopy for Selected Sets](#)

[Course Info](#) [Edit](#)

MAIN MENU

- Courses
- Homework Sets**
- User Settings
- Grades
- Instructor Tools
 - Classlist Editor
 - Hmwk Sets Editor
 - Library Browser
 - Statistics
 - Student Progress
 - Scoring Tools
 - Email
 - File Manager
 - Course Configuration
 - Help
- [Report bugs](#)

Page generated at 08/19/2017 at 04:35pm EDT

WeBWork © 1996-2016 | theme: math4 | ww_version: 2.12 | pg_version: 2.12 | The WeBWork Project

Math 1553

About the Course

Evaluations

- ▶ Homework
 - due at 11:59 pm on Wednesdays
 - completed via WebWork
 - two lowest dropped, no late hw
- ▶ Quiz
 - in Recitation on Fridays
 - covers material on the Homework
 - lowest dropped
- ▶ Three Midterms
 - Sep 22/Oct 20/Nov 17
 - Please tell me about Rosh Hashanah conflicts
- ▶ One common, cumulative Final
 - Dec 12
- ▶ One (small) Writing Project
- ▶ Participation
 - Clicker Polls
 - get the Piazza app for Wed

Not your High School Math Class

Your previous math courses probably focused on how to do computations:

- ▶ Compute the derivative of $\sin(\log x) \cos(e^x)$.

In this course:

- ▶ About half the material focuses on how to do linear algebra computations—that is still important.
- ▶ The other half is on *conceptual* understanding of linear algebra.

Advice, etc.

- ▶ Keep up with the definitions
- ▶ Come to office hours
- ▶ Sit in front, participate
- ▶ If you are having a problem, talk to me
- ▶ No devices in class unless instructed
- ▶ Be polite in your emails/posts

Introduction to Linear Algebra

Motivation and Overview

Linear

Algebra

- ▶ from al-jabr (Arabic), meaning reunion of broken parts
- ▶ 9th century Abu Ja'far Muhammad ibn Muso al-Khwarizmi

Why a whole course?

Engineers need to solve *lots* of equations in *lots* of variables.

$$3x_1 + 4x_2 + 10x_3 + 19x_4 - 2x_5 - 3x_6 = 141$$

$$7x_1 + 2x_2 - 13x_3 - 7x_4 + 21x_5 + 8x_6 = 2567$$

$$-x_1 + 9x_2 + \frac{3}{2}x_3 + x_4 + 14x_5 + 27x_6 = 26$$

$$\frac{1}{2}x_1 + 4x_2 + 10x_3 + 11x_4 + 2x_5 + x_6 = -15$$

Often, it's enough to know some information about the set of solutions without having to solve the equations at all!

In real life, the difficult part is often in recognizing that a problem can be solved using linear algebra in the first place: need *conceptual* understanding.

Many engineering problems, no matter how huge, can be reduced to linear algebra:

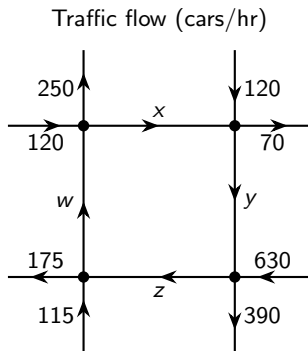
$$Ax = b \quad \text{or}$$

$$Ax = \lambda x$$

Applications of Linear Algebra

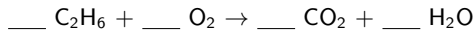
Civil Engineering: How much traffic flows through the four labeled segments?

~~~~~> system of linear equations:



# Applications of Linear Algebra

Chemistry: Balancing reaction equations



# Applications of Linear Algebra

Biology: In a population of rabbits. . .

- ▶ half of the new born rabbits survive their first year
- ▶ of those, half survive their second year
- ▶ the maximum life span is three years
- ▶ rabbits produce 0, 6, 8 rabbits in their first, second, and third years

If I know the population in 2017 (in terms of the number of first, second, and third year rabbits), then what is the population in 2018? or 2117?

## Applications of Linear Algebra

**Geometry and Astronomy:** Find the equation of a circle passing through 3 given points, say  $(1, 0)$ ,  $(0, 1)$ , and  $(1, 1)$ .

Hint: The general form of a circle is  $a(x^2 + y^2) + bx + cy + d = 0$ .

Very similar to computing the orbit of a planet:

$$ax^2 + by^2 + cxy + dx + ey + f = 0$$

# Applications of Linear Algebra

Google: “The 25 billion dollar eigenvector.” Each web page has some importance, which it shares via outgoing links to other pages

Stay tuned!



# Overview of the Course

- ▶ Solve the matrix equation  $Ax = b$ 
  - ▶ Solve systems of linear equations using matrices, row reduction, and inverses.
  - ▶ Solve systems of linear equations with varying parameters using parametric forms for solutions, the geometry of linear transformations, the characterizations of invertible matrices, and determinants.
  
- ▶ Solve the matrix equation  $Ax = \lambda x$ 
  - ▶ Solve eigenvalue problems through the use of the characteristic polynomial.
  - ▶ Understand the dynamics of a linear transformation via the computation of eigenvalues, eigenvectors, and diagonalization.
  
- ▶ Almost solve the equation  $Ax = b$ 
  - ▶ Find best-fit solutions to systems of linear equations that have no actual solution using least squares approximations.

