

Name SOLUTIONS

## Mathematics 1553

Quiz 4

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Section G1/Arjun G2/Talha G3/Athreya G4/Olivia G5/James (circle one!)

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1. Complete the following definition: *A basis for a subspace  $V$  of  $\mathbb{R}^n$  is...*

a set of linearly independent vectors  
that span  $V$ .

2. Let  $A$  be the matrix

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 0 \end{pmatrix}$$

and let  $T$  be the corresponding matrix transformation.

Compute  $T(v)$  where  $v = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$

$$\begin{pmatrix} 5 \\ 7 \\ 5 \end{pmatrix}$$

Find a vector in the codomain of  $T$  that is not in the range of  $T$ .

$$\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

Turn the page!

3. Let  $A$  be the matrix

$$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

Find a basis for the column space of  $A$ .

$$\left\{ \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \right\}$$

Find a basis for the null space of  $A$ .

$$\rightsquigarrow \begin{pmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \rightsquigarrow x + y + z = 0$$

$$\rightsquigarrow \begin{aligned} x &= -y - z \\ y &= y \\ z &= z \end{aligned}$$

$$\rightsquigarrow y \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix} + z \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}$$

$$\rightsquigarrow \left\{ \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} \right\}$$

What is the dimension of the null space of  $A$ ?

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