

# Practice Final Exam

⚠ This is a preview of the published version of the quiz

Started: Nov 30 at 11:16pm

## Quiz Instructions

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### Question 1

1 pts

If  $\{v_1, v_2, v_3\}$  is a linearly independent set of vectors in  $\mathbf{R}^4$  then  $\{v_1 + v_3, v_2 + v_3, v_3\}$  is linearly independent.

- True
- False

### Question 2

1 pts

Suppose  $A$ ,  $B$ , and  $C$  are  $n \times n$  matrices.

If  $A$  is invertible and  $AB = AC$ , then  $B = C$ .

- True
- False

### Question 3

1 pts

If  $A$  is a  $6 \times 4$  matrix, then the equation  $Ax = 0$  must have a non-trivial solution.

- True
- False

**Question 4****1 pts**

If an  $n \times n$  matrix  $A$  has two eigenvectors  $u$  and  $v$  corresponding to the same eigenvalue  $\lambda$ , then  $u$  must be a scalar multiple of  $v$ .

- True
- False

**Question 5****1 pts**

There are exactly two real values of  $c$  for which the distance between the vectors  $v$  and  $w$  in  $\mathbf{R}^3$  written below is equal to 4.

$$v = \begin{pmatrix} 1 \\ -2c \\ 1 \end{pmatrix}, \quad w = \begin{pmatrix} -1 \\ 2 \\ -1 \end{pmatrix}$$

- True
- False

**Question 6****1 pts**

Suppose  $A$  is an  $n \times n$  matrix and  $v$  is an eigenvector of  $A$  corresponding to the eigenvalue  $\lambda = -2$ .

Then  $2v$  is an eigenvector of  $A$  corresponding to the eigenvalue  $\lambda = -4$ .

True

False

### Question 7

1 pts

Suppose  $W$  is a subspace of  $\mathbf{R}^n$  and  $x$  is a vector in  $\mathbf{R}^n$ .

If the orthogonal projection of  $x$  onto  $W$  is the zero vector, then  $x$  is in  $W^\perp$ .

True

False

### Question 8

1 pts

Suppose  $A$  is an invertible  $3 \times 3$  matrix. Then the product of the second row of  $A$  and the third column of  $A^{-1}$  must equal 0.

True

False

### Question 9

1 pts

If  $A$  is an invertible matrix and  $\lambda$  is an eigenvalue of  $A$ , then  $\frac{1}{\lambda}$  is an eigenvalue of  $A^{-1}$ .

- True
- False

### Question 10

1 pts

Let  $T : \mathbf{R}^3 \rightarrow \mathbf{R}^2$  be the transformation given by  $T(x, y, z) = (x - y - z, x - y - z)$ .

Which of the following is true about  $T$ ?

- $T$  is neither one-to-one nor onto.
- $T$  one-to-one but not onto.
- $T$  is onto but not one-to-one.
- $T$  is one-to-one and onto.

### Question 11

1 pts

Which one of the following is a subspace of  $\mathbf{R}^3$ ?

- The 1-eigenspace of  $\begin{pmatrix} 1 & 0 & 1 \\ 0 & 3 & -1 \\ 0 & 0 & 6 \end{pmatrix}$
- $\text{Nul} \begin{pmatrix} 1 & 0 & 1 & 1 \\ -2 & 3 & -1 & 2 \\ 0 & 0 & 6 & -7 \end{pmatrix}$

$\text{Col} \begin{pmatrix} 1 & 0 & 1 \\ -2 & 3 & -1 \\ 0 & 0 & 6 \\ -1 & 1 & 0 \end{pmatrix}$

The set of all  $(x, y, z)$  in  $\mathbf{R}^3$  satisfying  $x - y - z = 1$ .

None of these are subspaces of  $\mathbf{R}^3$

### Question 12

1 pts

Consider the following matrix  $A$  and its reduced row echelon form:

$$A = \begin{pmatrix} 1 & -2 & 4 \\ 0 & 0 & 1 \\ 1 & -2 & 3 \\ -2 & 4 & -8 \end{pmatrix} \xrightarrow{RREF} \begin{pmatrix} 1 & -2 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}.$$

Find a basis for  $\text{Nul}(A)$ .

$\left\{ \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right\}$

$\left\{ \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \right\}$

$\left\{ \begin{pmatrix} 1 \\ 0 \\ 1 \\ -2 \end{pmatrix}, \begin{pmatrix} 4 \\ 1 \\ 3 \\ -8 \end{pmatrix} \right\}$

$\left\{ \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} \right\}$

$\left\{ \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix} \right\}$

**Question 13****1 pts**

Suppose  $A$  is an invertible  $2 \times 2$  matrix and  $A^{-1} \begin{pmatrix} 1 \\ 3 \end{pmatrix} = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$ .

Find the values  $a$  and  $b$  so that  $A \begin{pmatrix} 2 \\ -1 \end{pmatrix} = \begin{pmatrix} a \\ b \end{pmatrix}$ .

$a =$

$b =$

**Question 14****1 pts**

Let  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  be the linear transformation satisfying

$$T \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \text{ and } T \begin{pmatrix} 4 \\ 0 \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}.$$

Which one of the following statements is true?

$T$  is one-to-one and onto.

$T$  is onto but not one-to-one.

$T$  is one-to-one but not onto.

$T$  is neither one-to-one nor onto.

**Question 15****1 pts**

Which of the following transformations are linear? Select all that apply.

- $T : \mathbf{R}^3 \rightarrow \mathbf{R}^3$  defined by  $T(x, y, z) = (x, y + 1)$ .
- $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  defined by  $T(x, y) = (2x - \sin(y), \pi x)$ .
- $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  defined by  $T(x, y) = (x \ln(2), y)$ .

**Question 16****1 pts**

Find the numbers  $a$  and  $b$  so that the following matrix is stochastic.

$$A = \begin{pmatrix} a & 1/3 \\ 1/8 & b \end{pmatrix}.$$

a =

b =

Enter each answer as a *fraction*.

**Question 17****1 pts**

Fill in the blanks:

If  $A$  is a  $3 \times 7$  matrix and  $B$  is a  $7 \times 4$  matrix, then the transformation  $T(x) = ABx$  has domain  $\mathbf{R}^k$  and codomain  $\mathbf{R}^p$ ,

where  $k =$   and  $p =$  .

### Question 18

1 pts

Suppose  $A$  and  $B$  are  $2 \times 2$  matrices satisfying  $\det(A) = -4$ ,  $\det(B) = 2$ .

Find  $\det(A^3 B^{-1})$

### Question 19

1 pts

Suppose that  $v$  and  $w$  are eigenvectors of  $A$  with eigenvalues  $3$  and  $-7$  respectively. Find  $A(2v + 7w)$  in terms of  $v$  and  $w$ .

$A(2v + 7w) =$    $v +$    $w$ .

### Question 20

1 pts

Let  $A = \begin{pmatrix} 1 & -2 \\ -2 & 1 \end{pmatrix}$  and  $B = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 2 & 2 \end{pmatrix}$ .



Which statement below is true?

- A and B are both diagonalizable
- A is diagonalizable, but B is not diagonalizable
- B is diagonalizable, but A is not diagonalizable
- Neither A nor B is diagonalizable

### Question 21

1 pts

Suppose  $\det \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix} = 3$ .

Find  $\det \begin{pmatrix} g & h & i \\ d & e & f \\ g - 2a & h - 2b & i - 2c \end{pmatrix}$ .

### Question 22

1 pts

Suppose that  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  is a linear transformation satisfying

$$T \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 6 \\ 4 \end{pmatrix} \text{ and } T \begin{pmatrix} 4 \\ 0 \end{pmatrix} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}.$$

Find  $T \begin{pmatrix} 2 \\ 1 \end{pmatrix}$ .

$\begin{pmatrix} 3 \\ 1 \end{pmatrix}$

$\begin{pmatrix} 2 \\ 3 \end{pmatrix}$

$\begin{pmatrix} 9 \\ 3 \end{pmatrix}$

$\begin{pmatrix} 3 \\ 5 \end{pmatrix}$

 None of these

$\begin{pmatrix} 3 \\ 2 \end{pmatrix}$

$\begin{pmatrix} 3 \\ 9 \end{pmatrix}$

$\begin{pmatrix} -3 \\ -5 \end{pmatrix}$

$\begin{pmatrix} -5 \\ -3 \end{pmatrix}$

**Question 23****1 pts**

Let  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  be the linear transformation of orthogonal projection onto the line  $y = -x/4$ .

Write the value of  $c$  so that  $T \begin{pmatrix} 8 \\ c \end{pmatrix} = \begin{pmatrix} 8 \\ c \end{pmatrix}$ .

**Question 24****1 pts**

Let  $B = \begin{pmatrix} 7 & -8 \\ 4 & -5 \end{pmatrix}$ . Write the eigenvalues of  $B$  in increasing order.

The smaller eigenvalue is , and the larger eigenvalue is

.

**Question 25****1 pts**

Let  $T : \mathbf{R}^3 \rightarrow \mathbf{R}^3$  be the transformation that reflects vectors across the  $yz$ -plane, and let  $A$  be the standard matrix for  $T$ .

Which one of the following statements is true?

- $\dim(\text{Nul}(A - I)) = 2$  and  $\dim(\text{Nul}(A + I)) = 1$
- $\dim(\text{Nul}(A - I)) = 1$  and  $\dim(\text{Nul}(A + I)) = 2$
- $\dim(\text{Nul}(A - I)) = 1$  and  $\dim(\text{Nul}(A + I)) = 1$
- $\dim(\text{Nul}(A)) = 2$  and  $\dim(\text{Nul}(A + I)) = 1$
- $\dim(\text{Nul}(A)) = 1$  and  $\dim(\text{Nul}(A + I)) = 2$
- None of these

**Question 26****1 pts**

Select the matrix below whose 7-eigenspace is a line.

$$\begin{pmatrix} 7 & 0 & 0 \\ 1 & 7 & 0 \\ 0 & 1 & 7 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 1 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 7 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 0 & 1 \\ 0 & 7 & 0 \\ 0 & 0 & 7 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 0 & 1 \\ 0 & 7 & 1 \\ 0 & 0 & 7 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 7 \end{pmatrix}$$

$$\begin{pmatrix} 7 & 0 & 0 \\ 1 & 7 & 0 \\ 0 & 0 & 7 \end{pmatrix}$$

**Question 27****1 pts**

Suppose  $W$  is a subspace of  $\mathbf{R}^n$  and  $\mathbf{x}$  is a vector in  $\mathbf{R}^n$  satisfying

$$\mathbf{x}_W = \begin{pmatrix} 7 \\ 0 \\ 0 \end{pmatrix} \text{ and } \mathbf{x}_{W^\perp} = \begin{pmatrix} 0 \\ 3 \\ -4 \end{pmatrix}.$$

What is the distance from  $\mathbf{x}$  to  $W$ ?

**Question 28**

1 pts

Suppose  $\mathbf{u}$  and  $\mathbf{v}$  are *orthogonal* vectors in  $\mathbf{R}^4$  satisfying  $\|\mathbf{u}\| = 2$  and  $\|\mathbf{v}\| = 3$ .

Calculate the dot product  $(3\mathbf{u} - \mathbf{v}) \cdot (2\mathbf{v})$

**Question 29**

1 pts

Suppose  $\mathbf{A}$  is a  $3 \times 2$  matrix,  $\mathbf{b}$  is a vector, and  $\hat{\mathbf{x}} = \begin{pmatrix} 4 \\ 0 \end{pmatrix}$  is a least-squares solution to  $\mathbf{A}\mathbf{x} = \mathbf{b}$ .

Which one of the following statements must be true?

- $\begin{pmatrix} 4 \\ 0 \end{pmatrix}$  is the orthogonal projection  $\mathbf{b}$  onto  $\text{Col}(\mathbf{A})$ .
- $\text{rank}(\mathbf{A}) = 2$
- $\mathbf{A} \begin{pmatrix} 4 \\ 0 \end{pmatrix}$  is the closest vector to  $\mathbf{b}$  in  $\text{Col}(\mathbf{A})$ .
- The closest vector to  $\mathbf{b}$  in  $\text{Col}(\mathbf{A})$  is  $\begin{pmatrix} 4 \\ 0 \end{pmatrix}$ .

**Question 30**

1 pts

Let  $W$  be the line  $x_2 = -3x_1$  in  $\mathbf{R}^2$ . Find the number  $a$  so that the orthogonal projection of  $\begin{pmatrix} a \\ 1 \end{pmatrix}$  onto  $W$  is the zero vector.

### Question 31

1 pts

Suppose a positive stochastic matrix  $A$  has 1-eigenspace equal to the span of  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ .

Let  $v = \begin{pmatrix} 50 \\ 10 \end{pmatrix}$ . As  $n$  gets large,  $A^n v$  approaches some vector  $\begin{pmatrix} a \\ b \end{pmatrix}$ . Find  $a$  and  $b$ .

$a =$

$b =$  .

### Question 32

1 pts

Let  $W = \text{Span} \left\{ \begin{pmatrix} 1 \\ 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 2 \\ 2 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} \right\}$ .

Find the dimension of  $W$ .

## Question 33

1 pts

Select the matrix  $A$  that satisfies

$$A \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ -1 \end{pmatrix}, \quad A \begin{pmatrix} 0 \\ 1 \\ 2 \end{pmatrix} = \begin{pmatrix} 0 \\ 2 \\ 4 \end{pmatrix}, \quad A \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ -3 \\ 0 \end{pmatrix}.$$

$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & -3 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix}^{-1}$

$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 2 & -3 \\ -1 & 4 & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix}^{-1}$

$\begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & -3 \end{pmatrix} \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 1 & 0 \end{pmatrix}^{-1}$

$\begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & -3 \end{pmatrix}^{-1} \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 0 & 1 & 0 \end{pmatrix}$

$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & -3 \end{pmatrix}^{-1} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 0 \end{pmatrix}$

None of these

## Question 34

1 pts

Find the value of  $h$  so that the following set of vectors is linearly dependent.

$$\left\{ \begin{pmatrix} h \\ 2 \\ 1 \end{pmatrix}, \begin{pmatrix} -3 \\ -2 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right\}$$

### Question 35

1 pts

Suppose  $T : \mathbf{R}^m \rightarrow \mathbf{R}^n$  and  $U : \mathbf{R}^n \rightarrow \mathbf{R}^m$  are linear transformations.

Which one of the following statements *must* be true?

- The transformation  $T \circ U$  has domain  $\mathbf{R}^n$  and codomain  $\mathbf{R}^n$ .
- If  $m > n$ , then  $T \circ U$  is not onto.
- $U$  is one-to-one if for every  $x$  in  $\mathbf{R}^n$ , there is a  $y$  in  $\mathbf{R}^m$  so that  $U(x) = y$ .

### Question 36

1 pts

Some *diagonalizable*  $6 \times 6$  matrix  $A$  has characteristic polynomial

$$\det(A - \lambda I) = (4 - \lambda)^3 \lambda^2 (-3 - \lambda).$$

What is the dimension of the null space of  $A$ ?

- 2
- 1
- 3



- 4
- 
- 5
- 
- 6
- 
- Not enough information to know the answer

**Question 37****1 pts**

Which one of the following matrices satisfies both of the following conditions?

1.  $\text{Col}(A)$  is a subspace of  $\mathbf{R}^4$ .
2.  $\text{Nul}(A)$  is the line  $x_2 = 8x_1$  in  $\mathbf{R}^2$ .

$A = \begin{pmatrix} -8 & 1 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix}$

$A = \begin{pmatrix} 1 & 8 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix}$

$A = \begin{pmatrix} -8 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}$

$A = \begin{pmatrix} 8 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}$

$A = \begin{pmatrix} 8 & 1 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix}$

$$A = \begin{pmatrix} 1 & -8 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix}$$

none of these

### Question 38

1 pts

Let  $W$  be subspace of  $\mathbf{R}^3$  consisting of all  $(x, y, z)$  satisfying  $x = y = z$ .

What is the dimension of  $W^\perp$ ?

### Question 39

1 pts

Let  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  be reflection across the y-axis, let  $U : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  be rotation counterclockwise by 90 degrees, and let  $V : \mathbf{R}^2 \rightarrow \mathbf{R}^2$

be reflection across the line  $y = -x$ .

Which one of the following transformations has standard matrix equal to

$$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}?$$

$T \circ U$

$U \circ T$

$T \circ V$

$V \circ T$

$U \circ V$

$V \circ U$

**Question 40****1 pts**

Let  $A = \begin{pmatrix} -1 & 2 \\ 1 & 1 \\ 2 & -1 \end{pmatrix}$ .

Find the value of  $a$  so that  $(\text{Col } A)^\perp = \text{Span} \left\{ \begin{pmatrix} a \\ -1 \\ 1 \end{pmatrix} \right\}$ .

**Question 41****1 pts**

Suppose  $A$  is the matrix that implements reflection across the line  $y = -4x$  in  $\mathbf{R}^2$ . Which of the following statements is true?

- $A$  is invertible and diagonalizable.
- $A$  is invertible but is not diagonalizable.
- $A$  is diagonalizable but not invertible.
- $A$  is neither invertible nor diagonalizable.

**Question 42****1 pts**

Let  $W$  be the subspace of  $\mathbf{R}^3$  consisting of all  $(x, y, z)$  in  $\mathbf{R}^3$  satisfying  $x - 3y - z = 0$ , and let  $B$  be the matrix for orthogonal projection onto  $W$ .

Which one of the following statements must be true? If none must be true, select "none of these" as your answer.

$\text{rank}(B) = 1$

$B \begin{pmatrix} 4 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 4 \\ 1 \\ 1 \end{pmatrix}$

$W^\perp$  is a plane in  $\mathbf{R}^3$

The 1-eigenspace of  $B$  is 1-dimensional.

None of these

### Question 43

1 pts

Suppose  $A$  is a  $4 \times 4$  matrix whose entries are real numbers, and suppose  $1 + i$  and  $2 - i$  are eigenvalues of  $A$ .

Which statement below must be true? If none must be true, select "none of these" as your answer.

$A$  has no real eigenvalues.

$\det(A) = 0$

The equation  $Ax = b$  is inconsistent for some  $b$  in  $\mathbf{R}^4$

$A$  is a positive stochastic matrix.

none of these

## Question 44

1 pts

Which of the following gives least-squares line  $y = Cx + D$  for the data points  $(0, 1)$ ,  $(2, -2)$ , and  $(3, 2)$ ?

- We get C and D by solving

$$\begin{pmatrix} 0 & 2 & 3 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 2 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} 0 & 2 & 3 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ -2 \\ 2 \end{pmatrix}$$

- We get C and D by solving

$$\begin{pmatrix} 0 & 1 \\ 2 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} 0 & 2 & 3 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} 0 & 2 & 3 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ -2 \\ 2 \end{pmatrix}$$

- We get C and D by solving

$$\begin{pmatrix} 0 & 1 \\ 2 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} 0 & 2 & 3 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ -2 \\ 2 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 2 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix}$$

- We directly solve

$$\begin{pmatrix} 0 & 1 \\ 2 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 2 \end{pmatrix}$$

- We get C and D by solving

$$\begin{pmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ 2 & 1 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 2 \\ 3 \end{pmatrix}$$

- We get C and D by solving

$$\begin{pmatrix} 1 & 1 & 1 \\ 0 & 2 & 3 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 1 & 2 \\ 1 & 3 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 \\ 0 & 2 & 3 \end{pmatrix} \begin{pmatrix} 1 \\ -2 \\ 2 \end{pmatrix}$$

**Question 45****1 pts**

Consider an internet with 4 pages.

Page 1 links only to page 2.

Page 2 links to pages 1 and 3.

Page 3 links to pages 2 and 4.

Page 4 links to pages 1, 2, and 3.

What is the importance matrix (also known as Google matrix) for this internet?

$$A = \begin{pmatrix} 0 & 1/2 & 0 & 1/3 \\ 1 & 0 & 1/2 & 1/3 \\ 0 & 1/2 & 0 & 1/3 \\ 0 & 0 & 1/2 & 0 \end{pmatrix}$$

$$A = \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1/2 & 0 & 1/2 & 0 \\ 0 & 1/2 & 0 & 1/2 \\ 1/3 & 1/3 & 1/3 & 0 \end{pmatrix}$$

$$A = \begin{pmatrix} 1 & 1 & 0 & 0 \\ 1/2 & 1 & 1/2 & 0 \\ 0 & 1/2 & 1 & 1/2 \\ 1/3 & 1/3 & 1/3 & 1 \end{pmatrix}$$

$$A = \begin{pmatrix} 1 & 1/2 & 0 & 1/3 \\ 1 & 1 & 1/2 & 1/3 \\ 0 & 1/2 & 1 & 1/3 \\ 0 & 0 & 1/2 & 1 \end{pmatrix}$$

$$A = \begin{pmatrix} 1/2 & 1/3 & 0 & 1/4 \\ 1/2 & 1/3 & 1/3 & 1/4 \\ 0 & 1/3 & 1/3 & 1/4 \\ 0 & 0 & 1/3 & 1/4 \end{pmatrix}$$

**Question 46****1 pts**

Let  $T$  be a linear transformation such that  $T \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}$  and

$T \begin{pmatrix} 1 \\ -1 \end{pmatrix} = \begin{pmatrix} 0 \\ -1 \\ -2 \end{pmatrix}$ . Then,  $T \begin{pmatrix} 2 \\ 0 \end{pmatrix} = \begin{pmatrix} a \\ b \\ c \end{pmatrix}$ , where  $a =$  ,

$b =$   and  $c =$  .

**Question 47****1 pts**

What is the determinant of  $\begin{pmatrix} 1 & 0 & -1 & 0 & 0 & 15 \\ 0 & 7 & 5 & 0 & 19 & 0 \\ 0 & 0 & -2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 \end{pmatrix}$  ?

**Question 48****1 pts**

Suppose that  $A$  is a  $6 \times 7$  matrix and  $B$  is a  $7 \times 6$  matrix such that  $AB$  is the  $6 \times 6$  identity matrix. Is  $BA$  equal to the  $7 \times 7$  identity matrix?

## Question 49

1 pts

Let  $S$  be a region in the plane with area 3. Let  $T$  be the linear transformation  $T(x_1, x_2) = (x_1 + x_2, x_1 - x_2)$ . What is the area of  $T(S)$ ?

## Question 50

1 pts

You are tasked with uncovering information about a secret matrix, some of whose entries are hidden:

$$A = \begin{pmatrix} -1 & 0 & ? \\ ? & 4 & ? \\ ? & 0 & 0 \end{pmatrix}$$

(the "?" represent hidden entries). Given that  $\text{rank}(A) = 2$ , how many distinct eigenvalues does  $A$  have?

 0 1 2 3

Not saved

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