

Math 1553 Worksheet §3.2, 3.3

1. Which of the following transformations  $T$  are onto? Which are one-to-one? If the transformation is not onto, find a vector not in the range. If the transformation is not one-to-one, find two vectors with the same image.

a) Counterclockwise rotation by  $32^\circ$  in  $\mathbf{R}^2$ .

b) The transformation  $T : \mathbf{R}^3 \rightarrow \mathbf{R}^2$  defined by  $T(x, y, z) = (z, x)$ .

c) The transformation  $T : \mathbf{R}^3 \rightarrow \mathbf{R}^2$  defined by  $T(x, y, z) = (0, x)$ .

d) The matrix transformation with standard matrix  $A = \begin{pmatrix} 1 & 6 \\ -1 & 2 \\ 2 & -1 \end{pmatrix}$ .

2. On your computer, go to the [Interactive Transformation Challenge](#)! Complete the Zoom, Reflect, and Scale challenges. If you complete a challenge in the optimal number of steps, the interactive demo will congratulate you. See if you can complete each of these challenges in the optimal number of steps.
  
3. The second little pig has decided to build his house out of sticks. His house is shaped like a pyramid with a triangular base that has vertices at the points  $(0, 0, 0)$ ,  $(2, 0, 0)$ ,  $(0, 2, 0)$ , and  $(1, 1, 1)$ .

The big bad wolf finds the pig's house and blows it down so that the house is rotated by an angle of  $45^\circ$  in a counterclockwise direction about the  $z$ -axis (look downward onto the  $xy$ -plane the way we usually picture the plane as  $\mathbf{R}^2$ ), and then projected onto the  $xy$ -plane. Find the standard matrix  $A$  for the transformation  $T$  caused by the wolf.