

Name Prof. M

## Mathematics 2602

Quiz 2

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1. Rephrase the following proposition as an English sentence. Do not use “for all” or “there exists” in your answer.

$$\forall y \exists x (x^3 = y) \quad x, y \in \mathbb{R}$$

Every real number has a cube root.

2. Rephrase the following proposition as an English sentence. Do not use “for all” or “there exists” in your answer.

$$\exists x \exists y ((3x + 2y = 34) \wedge (x + y = 12)) \quad x, y \in \mathbb{R}$$

The lines  $3x + 2y = 34$  and  $x + y = 12$   
intersect.

3. Determine the truth values of the following propositions.

•  $\forall y \exists x (x^3 = y) \quad x, y \in \mathbb{R}$

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•  $\exists x \exists y ((3x + 2y = 34) \wedge (x + y = 12)) \quad x, y \in \mathbb{R}$

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•  $\exists x \forall y ((xy > 0) \wedge (y^2 + x = x)) \quad x, y \in \mathbb{R}$

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